## Rocket Trajectory Analysis

You will set up a numerical simulation to predict your rocket trajectory in this activity.

You will need:

- **D** Rocket and engine specifications (a computer connected to the internet is useful)
- □ Spreadsheet or calculator
- □ Sharp mind and pencil

## **Flight Simulations**

You need to have some general specifications prior to setting up your numerical simulation.

- □ Rocket mass, Engine mass, Fuel mass and Engine Time-Thrust data.
  - Comprehensive thrust vs time curve raw data can be found at <u>http://www.thrustcurve.org/</u>
  - General information from Estes <u>http://www.estesrockets.com</u> including Time-Thrust curves from Estes <u>http://www.estesrockets.com/images/page%2033.pdf</u> and Engine Specifications <u>http://www.estesrockets.com/images/page%2034.pdf</u>

You will use the basic laws of motion and a spreadsheet to calculate height as a function of time. Each column in your spreadsheet will be a different quantity:

- □ Time (pick a small increment you can always change it if it is not small enough or too small)
- $\Box Height: y_{new} = y_{old} + v_{avg}^* \Delta t$
- $\square Velocity: v_{new} = v_{old} + a^* \Delta t$
- $\Box \text{ Acceleration: } a = \Sigma F/m(t)$
- $\square$  Forces:  $F_{thrust},$   $F_{gravity}$  and  $F_{drag}$
- $\square Mass: m=m_{rocket}+m_{engine}+m_{fuel}(t)$ 
  - Let  $m_{fuel}$  be used up linearly over the time it takes the engine to burn typically 0.7 seconds so you could say  $m_f=m_o(0.7-t_i)/0.7$  where  $m_o$  is the initial mass of the fuel.
- $\Box \text{ Drag: } F_{\text{drag}} = 0.5 C_v \rho A v^2$ 
  - $\circ$   $\tilde{C}_v$ , the drag coefficient, is typically 0.7 to 1.4
  - $\circ$   $\rho$  is the density of air 1.29 kg/m<sup>3</sup>
  - A is the cross section of your rocket (make sure to get the units correct)

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## **On-line Flight Simulation Tools**

Feel free to use on-line tools to compare to your own calculations.

- D NASA
  - o Rocket Engine Performance <u>http://www.grc.nasa.gov/WWW/K-12/airplane/rktengperf.html</u>
  - o Model Rocket Index http://www.grc.nasa.gov/WWW/K-12/airplane/shortr.html
- □ Model Rocket Altitude Predictor (<u>http://webalt.markworld.com/</u>) at <u>http://www.markworld.com/</u>
- □ Rocket Simulation (how to write a numerical simulation) <u>http://my.execpc.com/~culp/rockets</u>